

Practice Test #1

Polynomials

Please Note: Use calculator where necessary.

Max Marks:

Time: 1800 sec

1. Factor the following polynomials completely, and state all the zeroes. [2+2]

(a) $2x^4 - x^3 - x^2$

(b) $x^6 - 1$

2. (a) Show that if $P(x) = ax^4 + bx^3 + cx^2 + dx + e$ is **even**, then $b = d = 0$. [3+3]

(b) Show that if $Q(x) = ax^5 + bx^4 + cx^3 + dx^2 + ex + f$ is **odd**, then $b = d = f = 0$.

3. Sketch graphs of the following polynomials, clearly indicating all intercepts with the axes:

(a) $y = (2-x)^2(5-x)$ [3+3]

(b) $f(x) = -2x^2 + 9x - 7$

4. Find the coordinates of the points where the graph of $y = p(x)$, $p(x) = x^4 - 2x^2 + 1$, crosses the x- and y-axes, and hence sketch the graph. [4]

5. (a) Find the quotient and remainder when $x^4 - 2x^3 + x^2 - 5x + 7$ is divided by $x^2 + x - 1$. [3+3]

(b) Find **a** and **b** if $x^4 - 2x^3 + x^2 + ax + b$ is exactly divisible by $x^2 + x - 1$.

6. (a) Show that the equation of the normal to the curve $x^2 = 4y$ at the point $(2t, t^2)$ is $x + ty - 2t - t^3 = 0$. [6+2]

(b) If the normal passes through the point $(-2, 5)$, find the value of **t**.

7. The polynomial $W(x)$ is divided by $(x + 4)(x - 3)$.

Find the remainder, given that $W(-4) = 11$ and $W(3) = -3$. [4]

***** Good Luck *****